

# Probing the Anomalous FCNC Interactions in Top-Higgs Final State and Charge Ratio Approach

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## Abstract

We study the anomalous production of a single top quark in association with a Higgs boson at the LHC originating from flavor changing neutral current (FCNC) interactions in  $tqg$  and  $tqH$  vertices. We derive the discovery potentials and 68% C.L. upper limits considering leptonic decay of the top quark and the Higgs boson decay into a  $b\bar{b}$  pair with  $10 \text{ fb}^{-1}$  integrated luminosity of data in proton-proton collisions at the center-of-mass energy of 14 TeV. We propose a charge ratio for the lepton in top quark decay in terms of lepton  $p_T$  and  $\eta$  as a strong tool to observe the signal. In particular, we show that the charge ratio increases significantly at large  $p_T$  of the charged lepton. While the main background from  $t\bar{t}$  is nearly charge symmetric and  $W + jets$  background has much smaller charge ratio with respect to the signal. We show that this feature can also be used in the probe of anomalous single top production with a  $Z$ -boson or a photon which are under the attention of the experimental collaborations.

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# 1 Introduction

In view of the top quark large mass, it is a unique place to probe the dynamics that breaks the electroweak gauge symmetry. Several properties of the top quark have been measured and studied using the data collected with the LHC experiments at the center-of-mass energies of 7 and 8 TeV as well as the Tevatron experiments. The top quark interacts with other Standard Model (SM) particles via gauge and Yukawa interactions. So far, many remarkable results have come out of the LHC and Tevatron experiments including the top quark interactions in both electroweak and strong sectors. It is worthy to mention that both the ATLAS and the CMS experiments have measured several properties of the top quark with high precision [1], [2]. In particular, the cross section for single top production has been measured with a precision of less than 15% [3] and the present measurement of the top pair rate is better than 10% [4]. Undoubtedly, it is expected that the top quark properties will be measured with more precision using more amount of data and in the next phase of the LHC with collisions at 13 or 14 TeV.

Flavor Changing Neutral Current (FCNC) couplings are strongly suppressed in top sector at tree level in the SM framework by Glashow-Iliopoulos-Maiani (GIM) mechanism [5]. While the FCNC processes involving the top quark can appear in models beyond the SM. In particular, significant FCNC couplings of top quark with an up or charm quark and a gluon are predicted in several new physics models beyond the SM [6], [7], [8], [9], [10] [11], [12]. The anomalous FCNC couplings for top with an up-type quark (u,c) and a gluon can be described in a model independent effective Lagrangian way according to the following [13], [14]:

$$\mathcal{L} = \sqrt{2}g_s \sum_{q=u,c} \frac{\kappa_{tqg}}{\Lambda} \bar{t} \sigma^{\mu\nu} T_a (f_q^L P_L + f_q^R P_R) q G_{\mu\nu}^a + h.c. \quad (1)$$

Here  $P_L$  and  $P_R$  are chirality projection operators. In Eq.1,  $\Lambda$  is the energy scale which new physics appears and  $\kappa_{tqg}$  are real dimensionless parameters thus  $\frac{\kappa_{tqg}}{\Lambda}$  are the strength of the couplings. The parameters  $f_q^L$  and  $f_q^R$  are chiral parameters with the normalization of  $|f_q^L|^2 + |f_q^R|^2 = 1$ .

There are many analyzes in search for the anomalous  $tqg$  and other anomalous couplings related to the top interaction in the literature [15], [16], [18], [19], [20], [21]. The CDF and D0 experiments at the Tevatron have searched for these FCNC couplings [22], [23]. The 95% confidence level limits on the anomalous FCNC couplings have been found to be:

$$\frac{\kappa_{tug}}{\Lambda} < 0.013 \text{ TeV}^{-1}, \quad \frac{\kappa_{teg}}{\Lambda} < 0.057 \text{ TeV}^{-1} \quad (2)$$

Recently, the ATLAS experiment set 95% C.L. upper limits on the strong FCNC couplings using  $14.2 \text{ fb}^{-1}$  of 8 TeV data. In the ATLAS search for the FCNC events in  $tqg$  vertex,

the production of a single top quark with or without another light quark or gluon are considered [24]. The extracted limits are the most stringent limits on these couplings:

$$\frac{\kappa_{tug}}{\Lambda} < 5.1 \times 10^{-3} \text{ TeV}^{-1}, \quad \frac{\kappa_{tcg}}{\Lambda} < 1.1 \times 10^{-2} \text{ TeV}^{-1} \quad (3)$$

The FCNC anomalous interaction  $tqg$  can lead to production of a top quark in association with a  $Z$ -boson. In [17], a search for the top quark anomalous couplings has been performed through the search for the final state of a single top quark in association with a  $Z$ -boson at the LHC with the CMS detector. This search has been performed using  $5 \text{ fb}^{-1}$  of proton-proton collisions at 7 TeV data. The 95% C.L. observed upper limits on the anomalous couplings of the effective model are found to be:

$$\frac{\kappa_{tug}}{\Lambda} < 0.1 \text{ TeV}^{-1}, \quad \frac{\kappa_{tcg}}{\Lambda} < 0.35 \text{ TeV}^{-1} \quad (4)$$

Lower cross section of this process and smaller amount of data is the reason that these bounds are looser than the bounds with respect to the bounds indicated in Eq.2, Eq.3. However, performing such an analysis is necessary to check the consistency of all results in searches for FCNC. There is another detailed study for the anomalous interactions of  $tqg$  using the  $tZ$  channel at the LHC with  $20 \text{ fb}^{-1}$  of 8 TeV collisions in [18]. The  $3\sigma$  discovery ranges obtained in this study are as follows:

$$\frac{\kappa_{tug}}{\Lambda} > 0.09 \text{ TeV}^{-1}, \quad \frac{\kappa_{tcg}}{\Lambda} > 0.31 \text{ TeV}^{-1} \quad (5)$$

The discovery of a new Higgs-like particle with a mass of around 125 GeV by the ATLAS and CMS experiments at the LHC [25], [26] has opened a new window in searches for different properties of SM particles. In particular, because of the large coupling of the Higgs boson with top quark, the top quark properties could be studied in channels where a Higgs boson is also present. In this work, we perform a search for anomalous top interaction of  $tqg$  by studying a signature consisting of a Higgs boson and a single top quark. We perform the analysis for 10 and  $100 \text{ fb}^{-1}$  of the LHC proton-proton collisions at the center-of-mass energy of 14 TeV. We investigate the final state of three b-jets where the top quark decays to a charged lepton (muon or electron), neutrino and a b-quark and the Higgs boson decays into a  $b\bar{b}$  pair. The representative Feynman diagram of the signal process including the decay chain is shown in Fig.1 (left). In the final state we expect only one charged lepton, missing energy and three  $b$ -tagged jets. We find the parameter regions where the LHC may be able to observe the signal, otherwise upper limits are set on the anomalous couplings. The real data of the LHC could be used in search for the anomalous  $tqg$  couplings in this channel

since it provides really reasonable results in comparison with the already obtained results from other channels even with a simple set of cuts. In order to improve the sensitivity to the  $tqg$  anomalous couplings, the  $tH$  channel results can be combined with both the FCNC single top quark and top pair production modes.

It is remarkable that for our favorite signal the radiation of a Higgs boson does not change the spin direction of the top quark. Therefore, if the anomalous interactions are quite left-handed ( $f_q^L = 1, f_q^R = 0$ ) or right-handed ( $f_q^L = 0, f_q^R = 1$ ), the top quark is produced with the spin direction parallel to the incident quark momentum direction for the left-handed case and opposite to the incident quark momentum for right-handed case. The chirality information is transferred to the decay products of the top quark, accordingly by a careful study of the charged lepton angular distribution, the type of interaction (left-handed or right-handed couplings) could be determined. Among the channels by which we can probe the anomalous  $tqg$  couplings, the direct top production [15] and top plus Higgs channel ( $u(c) + g \rightarrow t + H$ ) provide the possibility to determine the chirality nature of these couplings.

It is interesting to note that in addition to the effective FCNC Lagrangian in the vertex of  $tqg$ , introduced in Eq.1, the anomalous FCNC interaction in the  $tqH$  vertex leads to production of a single top quark in association with a Higgs boson as well. This is illustrated by a Feynman diagram in the right-side of Figure 1 where flavor changing interaction of the top quark and light quark involves a Higgs boson. The anomalous FCNC interaction  $tqH$  can be parametrized as the following [7]:

$$\mathcal{L} = \frac{g}{2\sqrt{2}} \sum_{q=u,c} g_{tqH} \bar{q}(g_{tqH}^v + g_{tqH}^a \gamma_5) t H + h.c. \quad (6)$$

where the real coefficient  $g_{tqH}$  (with  $q = u, c$ ) denotes the strength of the anomalous coupling. The coefficients  $g_{tqH}^v, g_{tqH}^a$  are in general complex numbers with the normalization  $|g_{tqH}^v|^2 + |g_{tqH}^a|^2 = 1$ . The 95% C.L. upper bounds on the FCNC  $tqH$  couplings derived from the low energy experiments with the Higgs boson mass in the interval of 115 to 170 GeV are [27], [28]:

$$g_{tuH} < 0.363 - 0.393, \quad g_{tcH} < 0.270 - 0.319 \quad (7)$$

In [16] the anomalous production of a single top quark with a Higgs boson via the FCNC interaction of  $tqH$  has been studied at the LHC including complete QCD next-to-leading order corrections. The  $3\sigma$  exclusion upper limits on the anomalous couplings with the Higgs boson mass of 125 GeV based on  $10 \text{ fb}^{-1}$  of the integrated luminosity have been found to be:

$$g_{tuH} < 0.121, \quad g_{tcH} < 0.233 \quad (8)$$

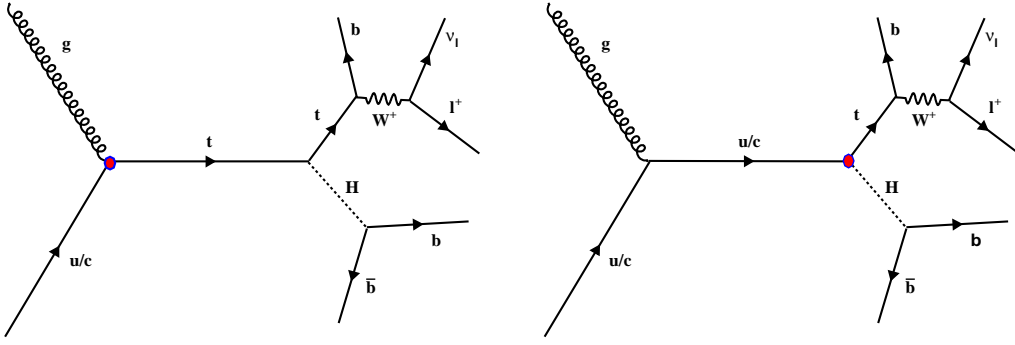


Figure 1: The representative Feynman diagram for production of a top quark in association with a Higgs boson including the decay chain with leptonic top quark decay and Higgs decay into a  $b\bar{b}$  pair.

It is notable that both anomalous couplings  $tqg$  and  $tqH$  are arising from dimension-six operators. Therefore, it makes sense to consider both anomalous interactions together. The Feynman diagrams depicted in Figure 1 can be studied simultaneously that leads to an interference term. In this paper, we study the single top plus a Higgs boson final state once in the presence of only  $tqg$  couplings and once in the presence both  $tqg$  and  $tqH$  anomalous interactions.

The organization of this paper is as follows. Next section is devoted to events simulation for signal (left diagram of Figure 1) and backgrounds and analysis. In section 3, we obtain the discovery potential and 68% C.L. upper limits on the anomalous couplings from this channel and discuss the results. Section 4 presents a simultaneous probe of  $tqg$  and  $tqH$ . In section 5, we will discuss a way based on the leptonic charge ratio to discriminate between signal and backgrounds and to distinguish between  $tug$  and  $tcg$  couplings. In particular, we look at the charge ratio as a function of  $p_T$  and  $\eta$  of the charged lepton for signal and background processes. Finally, conclusions are presented in section 6.

## 2 Event Simulation and Selection

In this section, we define the signal and backgrounds processes and describe the simulation method, the event selection and reconstruction of the final state. The process of signal is taken as the single top plus a Higgs boson followed by the leptonic top quark decay and the Higgs boson decay into a  $b\bar{b}$  pair. The Feynman diagram of production and decay chain is presented in Figure 1. The main background processes are  $Wb\bar{b}j$ ,  $Wjjj$ ,  $WZj$ , and  $t\bar{t}$ . For both signal and the background processes, the MADGRAPH 5 package [29] has been used

to generate the hard scattering matrix elements with the CTEQ6 [30] as parton distribution function. The parton level events are passed through PYTHIA 8 [31] for showering. The jet reconstruction is then performed by FASTJET package [32] using an anti- $k_t$  algorithm with the cone size of  $R = 0.5$  [33]. Where  $R = \sqrt{(\Delta\eta)^2 + (\Delta\phi)^2}$ , with  $\eta = -\ln \tan(\theta/2)$ . The parameters  $\eta$  and  $\phi$  are the polar and azimuthal angles w.r.t the  $z$ -axis. In this analysis, we focused on the LHC run with the center-of-mass energy of  $\sqrt{s} = 14 \text{ TeV}$  for the integrated luminosities of  $10 \text{ fb}^{-1}$  and  $100 \text{ fb}^{-1}$ . In order to simulate the signal events, the effective Lagrangian of Eq.1 has been implemented within the FEYNRULES package [34], [35] then imported the model to a UFO module [36] and then inserted to the MADGRAPH 5. The cross sections has been found to be consistent with COMPHEP package [37], [38]. In this analysis, we only concentrate on the case that  $f_q^L = f_q^R = 1$ . The signal is generated with top quark decay leptonically (muon and electron) and the Higgs boson decaying into  $b\bar{b}$ . The  $t\bar{t}$  background is generated in semi-leptonic decay mode. The  $Wb\bar{b}j$ ,  $Wjjj$ ,  $WZj$  are generated with again leptonic decay of the  $W$ -boson and for the latter one the  $Z$ -boson decays into a  $b\bar{b}$ . To simulate b-tagging, a b-tagging efficiency of 60% is chosen for b-jets and a mis-tagging rate of 10% for other quarks. The effects of detector resolution are simulated through Gaussian energy smearing which is applied to jets and leptons with a standard deviation parameterized according to the following:

$$\frac{\sigma(E)}{E} = \frac{a}{\sqrt{E(\text{GeV})}} \oplus b \quad (9)$$

where  $\sigma(E)$  indicates the energy resolution at the energy value of  $E$ , the symbol  $\oplus$  represents a quadrature sum, and the energies are measured in GeV. For resolutions of jets (leptons) we take the values of ATLAS detector [39],  $a = 0.5(0.1)$  and  $b = 0.03(0.007)$ . It is notable that the electron and muon energy resolutions have different dependencies on the electromagnetic calorimetry and the charged particle tracking. Nevertheless, the uniform values for electromagnetic calorimetry energy resolution is used for the final state lepton. It is more conservative for the energies under consideration in the analysis than the capabilities of tracking. In order to trigger the events, every event is required to have at least one charged lepton passing through the cuts on the rapidity and transverse momentum. The typical value for charged lepton  $p_T$  cut is 25 GeV within the pseudorapidity range of  $|\eta| < 2.5$ . The missing transverse energy is required to be larger than 25 GeV. The jets are required to have  $p_T > 25 \text{ GeV}$  with pseudorapidities to be  $|\eta| < 2.5$ . The angular distance between the charged lepton and jets and all jets have to be  $\Delta R_{lj,jj} > 0.4$ . The cross section of signal

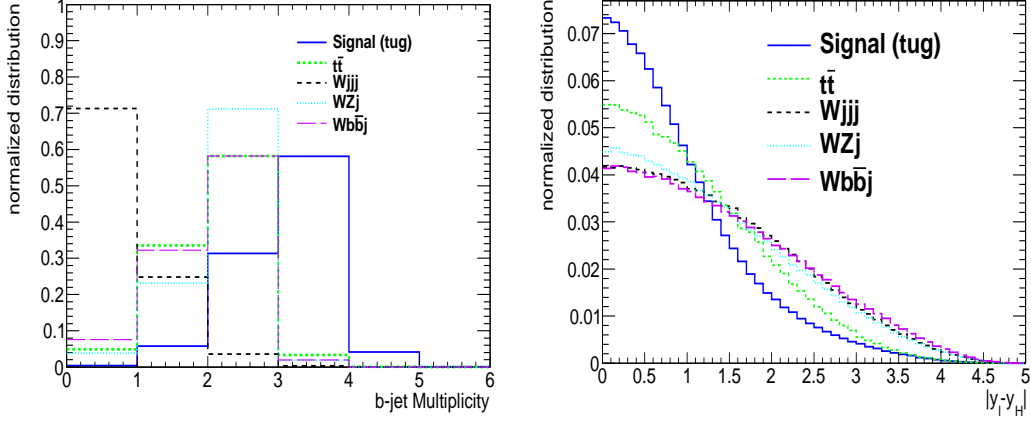


Figure 2: b-jet multiplicity distribution for signal and backgrounds (left) and the reconstructed distribution of  $|y_l - y_H|$  for signal and different backgrounds. The distributions are normalized to one.

after the above preliminary cuts including the branching ratios are:

$$\sigma(\kappa_{tug}/\Lambda) \text{ pb} = 5.60 \times \left[\frac{\kappa_{tug}}{\Lambda}\right]^2, \quad \sigma(\kappa_{tcg}/\Lambda) \text{ pb} = 1.05 \times \left[\frac{\kappa_{tcg}}{\Lambda}\right]^2 \quad (10)$$

where  $\kappa_{tqg}/\Lambda$  is in  $\text{TeV}^{-1}$ . The process  $Wjjj$  has the largest cross section which is 230.0 pb considering the cuts and branching ratios. The  $t\bar{t}$  cross section after the cuts and taking into account the branching ratios is 34.35 pb. The cross sections of  $Wb\bar{b}j$  and  $WZj$  processes are 2.33 pb and 0.138 pb, respectively. In order to reconstruct the top quark and Higgs boson in the final state, first we require to have only three b-tagged jets in each event. The plot in the left side of Fig. 2 shows the b-jet multiplicity in signal and different background events. As can be seen the requirement of only three b-tagged jets is useful to reduce the contribution of the backgrounds. We specifically apply such a requirement to suppress the large contributions of background events originating from  $Wjjj$ . To reconstruct the top quark, the full momentum of the neutrino is needed. The missing transverse energy is taken as the transverse component of the neutrino momentum. The  $z$ -component of the neutrino momentum is obtained by using the  $W$ -boson mass constraint:  $(p_l + p_{T,\nu} + p_{z,\nu})^2 = m_W^2$ . In most cases, there are two solutions for the  $p_{z,\nu}$ . As a result, the combination of the charged lepton and two neutrinos leads to two  $W$ -bosons which are combined with the three b-tagged jets separately. Among the six combinations, the combination which gives the closest mass to the top quark mass is selected. The other remaining two b-jets are combined to reconstruct the Higgs boson.

In order to suppress the backgrounds, we reject events with  $|m_{H,rec} - 125| > 15 \text{ GeV}$ . To reduce the contributions of the backgrounds and enhance the signal contribution, we

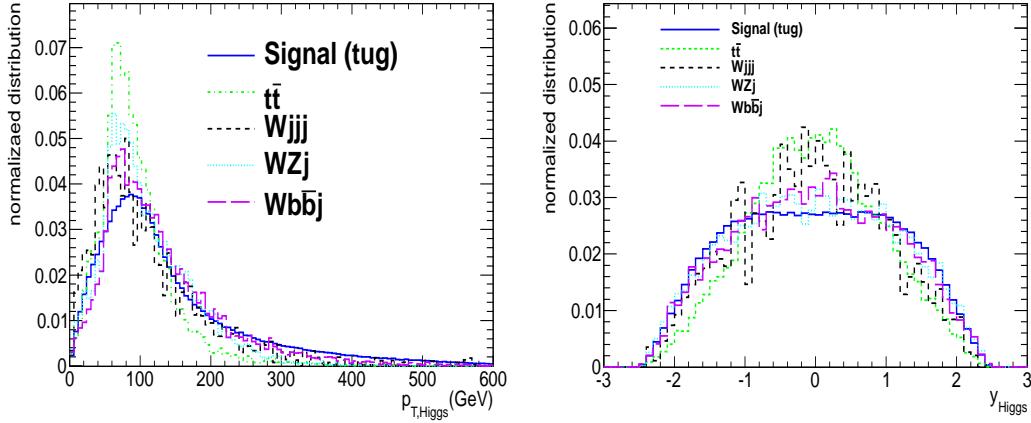


Figure 3: The transverse momentum of the reconstructed Higgs boson (left) and the rapidity distribution of the Higgs boson (right) for signal and backgrounds.

exploit some other kinematic distributions. In the right panel of Fig.2, the distribution of the difference between the pseudorapidities of the charged lepton and the reconstructed Higgs boson ( $|y_l - y_H|$ ) is shown. The signal events prefer to reside mostly at around zero while the backgrounds in particular the  $W + jets$  events have a more spread distribution and is extended up to around 5. Therefore, We require the events to satisfy  $|y_l - y_H| < 1.2$  condition to reduce the  $W + jets$  contributions. We use two more kinematic variables to suppress the backgrounds. In Fig.3, the transverse momentum and rapidity distributions of the reconstructed Higgs boson are depicted. From the left panel of Fig.3, we can see that in the  $p_{T,Higgs}$  distributions of  $Wb\bar{b}j$ ,  $Wjjj$ , and  $WZj$  the peaks are below 80 GeV while for the signal the peak is around 90-100 GeV. Therefore, we require that the transverse momentum of the Higgs boson to be greater than 100 GeV. As it can be seen in the right panel of Fig.3, for the signal process of  $u + g \rightarrow t + H$ , the Higgs bosons tend to reside also in the forward and backward regions while the main backgrounds of  $t\bar{t}$  and  $W + jets$  are mostly central. Since the up quark on average carries larger momentum with respect to gluon, the center-of-mass frame of the final state system is boosted along the direction of the initial up quark. We do not face with this situation for top pair events because the top pair events are mostly coming from gluon-gluon fusions which are symmetric. Only there is a small boost effect in top pair events due to quark anti-quark annihilation. We choose the events with  $|y_H| > 0.8$ . Because such an effect does not exist for the signal process of  $c + g \rightarrow t + H$ , we do not apply this cut for this process. In Fig.4, we show the reconstructed top quark mass after all cuts for signal and backgrounds with  $10 \text{ fb}^{-1}$  of integrated luminosity and with  $\kappa_{tug}/\Lambda = 0.1 \text{ TeV}^{-1}$ . It can be seen that top quark has been reconstructed well.



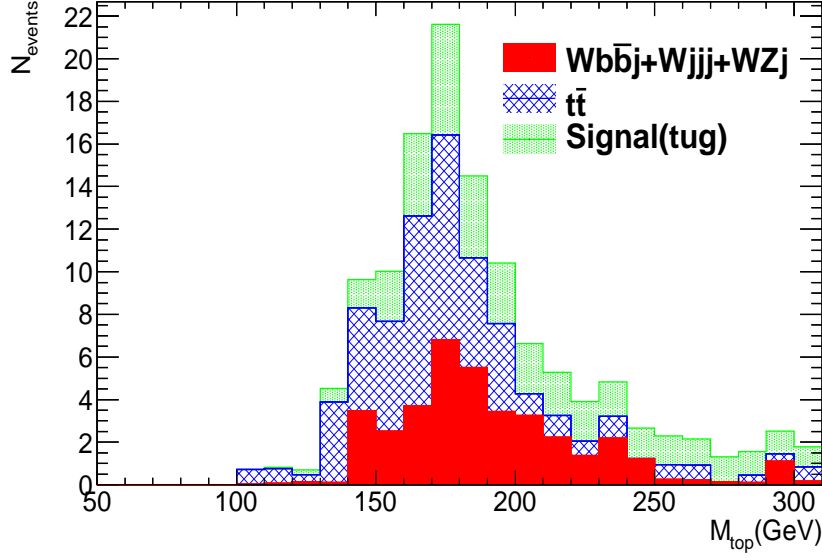


Figure 4: The reconstructed top mass distribution after all selection for  $10 \text{ fb}^{-1}$  of LHC at 14 TeV center-of-mass energy for the signal with  $\kappa_{tug}/\Lambda = 0.1 \text{ TeV}^{-1}$  and backgrounds.

### 3 Results

After applying all cuts which we explained in the previous section, we obtain the following efficiencies for signal ( $\frac{\kappa_{tug}}{\Lambda} = 0.1 \text{ TeV}^{-1}$ ),  $t\bar{t}$ ,  $Wb\bar{b}j$ ,  $Wjjj$ , and  $WZj$  respectively: 12%, 0.017%, 0.04%, 0.0023%, 0.071%. For the  $tcg$  signal the efficiency has been found to be 6%. It should be mentioned that the  $t\bar{t}$  process could also be considered as a source of top plus a Higgs boson. When one of the top quarks radiates a Higgs boson, the final state consists of  $t\bar{t} + H$ . Such events are unlikely to pass our selection. Because we require to have only one isolated lepton as well as exactly three b-jets in the event which do not allow such events to contribute to the signal. We calculate the  $3\sigma$  and  $5\sigma$  discovery reaches of the LHC for the anomalous couplings  $\frac{\kappa_{tug}}{\Lambda}$  and  $\frac{\kappa_{tcg}}{\Lambda}$  after the event selection according to  $S/\sqrt{B}$  formula. The  $3\sigma$  ( $5\sigma$ ) values for  $10 \text{ fb}^{-1}$  are summarized below:

$$\frac{\kappa_{tug}}{\Lambda} \geq 0.069 \text{ (0.088) } \text{TeV}^{-1}, \quad \frac{\kappa_{tcg}}{\Lambda} \geq 0.26 \text{ (0.34) } \text{TeV}^{-1} \quad (11)$$

We see a better sensitivity to  $\frac{\kappa_{tug}}{\Lambda}$  with respect to  $\frac{\kappa_{tcg}}{\Lambda}$  which is because of the fact that the parton density function of the charm quark is suppressed w.r.t the up quark.

The next-to-leading order QCD corrections to signal would improve the results however the NLO corrections for our favorite signal is not available. If we assume similar  $k$ -factor of 1.3 as direct top production ( $g + u(c) \rightarrow t$ ) [15] and  $g + u(c) \rightarrow t + Z$  [40], the results mentioned

above will improve up to the order of 10%. In case of finding no evidence for signal, upper limits can be set on the anomalous interaction parameters. To set the 68% C.L. limits, we use a simple  $\chi^2$  criterion from the distribution of  $|y_l - y_H|$  with  $10 \text{ fb}^{-1}$  of the integrated luminosity. We perform the  $\chi^2$  on this distribution because the signal and background shapes are different and therefore could lead to stronger limits. The  $\chi^2$  criterion is defined as:

$$\chi^2(\frac{\kappa_{u,c}}{\Lambda}) = \sum_{i=\text{bins}} \frac{(s_i - b_i)^2}{\Delta_i^2} \quad (12)$$

where  $s_i$  denotes the number of signal events in the  $i$ -th bin of the  $y_l - y_H$  distribution and  $b_i$  is the number background events predicted by the standard model in the  $i$ -th bin. The  $\chi^2$  criterion depends on anomalous couplings of  $\kappa_{u,c}/\Lambda$ . In the  $\chi^2$  definition,  $\Delta_i = b_i \sqrt{\delta_{stat}^2 + \delta_{sys}^2}$  where  $\delta_{stat}$  is the statistical uncertainty and  $\delta_{sys}$  denotes the term for considering systematic uncertainties. Systematic uncertainties from the top quark mass, PDF, factorization and renormalization scales, luminosity measurements and etc. are necessary for more realistic results. However, at this level of analysis it is difficult to give estimations of all systematics. Therefore, a combined systematic uncertainty of 10% is taken into account. The 68% C.L. upper limits on the anomalous FCNC couplings are found to be:

$$\frac{\kappa_{tug}}{\Lambda} \leq 0.014 \text{ TeV}^{-1}, \quad \frac{\kappa_{tcg}}{\Lambda} \leq 0.045 \text{ TeV}^{-1} \quad (13)$$

Certainly, these limits could be improved using advanced methods to separate signal from backgrounds such as neural networks [41] and boosted decision trees. The combination of the limits from this channel with other channels also can lead to tighter bounds on the anomalous couplings.

In this analysis, we have not considered QCD multijet events. Because of its huge cross section, a data-driven technique is needed to estimate the contribution of this background. However, it is expected that the contribution of this background is negligible after the requirement of one isolated lepton and the missing transverse energy. Furthermore, requiring three b-tagged jets that two of them must have a mass in the Higgs mass window is expected to suppress the QCD background.

The SM Single top plus Higgs,  $tZj$ , and  $t\bar{t}Z$  events can also be sources of backgrounds to our signal. The inclusive LO cross sections are 52 fb, 0.55 pb, and 1.02 pb, respectively. We have not included these backgrounds in the analysis due to very small cross sections. After including the branching ratios and applying the cuts, negligible number of events will be survived.

One of the main backgrounds to this analysis is  $W + jets$ . The requirement of exactly three b-jets suppresses this background dramatically. We expect that a full analysis with well developed algorithms for b-tagging provides more precise and reliable results. Therefore, a full detector analysis by the experimental collaborations is needed to confirm the results that we obtained in this analysis.

## 4 Simultaneous Probe of $tqg$ and $tqH$ Couplings

The final state of single top quark plus a Higgs boson can arise from both anomalous interactions  $tqg$  and  $tqH$ . Both anomalous couplings come from dimension six operators. Therefore, in the presence of both couplings the anomalous single top quark in association with a Higgs boson production cross section can be parameterised as:

$$\sigma(\frac{\kappa_{tqg}}{\Lambda}, g_{tqH})[\text{pb}] = c_{tqg} \times (\frac{\kappa_{tqg}}{\Lambda})^2 + c_{tqH} \times g_{tqH}^2 + c_{int.} \times \frac{\kappa_{tqg}}{\Lambda} \times g_{tqH} \quad (14)$$

where  $\kappa_{tqg}/\Lambda$  is in  $\text{TeV}^{-1}$  and  $g_{tqH}$  is dimensionless. The coefficients  $c_{tqg}$ ,  $c_{tqH}$ , and  $c_{int.}$  are determined with MADGRAPH. After the preliminary cuts described in section 2, the coefficients are  $c_{tu(c)g} = 5.6(1.05)$ ,  $c_{tu(c)H} = 0.09(0.01)$ , and  $c_{int.} = 0.46(0.2)$ . The numbers in parantheses denotes the coefficients for the  $tcg$  and  $tcH$  couplings. As it can be seen, the anomalous  $tqg$  coupling can have larger contribution to the production of a single top quark in association with a Higgs boson. After applying similar requirements to what explained in the previous section the  $3\sigma$  exclusion limits on the anomalous  $tqg$  and  $tqH$  are extracted. Figure 5 shows the  $3\sigma$  exclusion regions in the plane of  $(\kappa_{tqg}/\Lambda, g_{tqH})$  using  $10 \text{ fb}^{-1}$  of the integrated luminosity in proton-proton collisions at 14 TeV. In this plot, the smallest region shows the  $3\sigma$  region for the anomalous interactions  $tug$  and  $tuH$  and the bigger one is the allowed region for  $tcg$  and  $tcH$ . Because of the smaller contribution to the signal cross section looser bounds are obtained on the  $tqH$  couplings with respect to the  $tqg$  couplings.

## 5 Charge Ratio

One of the striking features of our signal, single top plus a Higgs boson production at the LHC, is asymmetry between top and anti-top rates. The cross section of top and anti-top quarks are different at the LHC for the process of  $g+u(\bar{u}) \rightarrow t(\bar{t})+H$  because of the difference between the  $u$ -quark and  $\bar{u}$ -quark parton distribution functions of proton. Since the  $c$ -quark and  $\bar{c}$ -quark parton distribution functions are similar, the rates of top and anti-top quarks from the process of  $g+c(\bar{c}) \rightarrow t(\bar{t})+H$  are expected to be similar. In leptonic top decay, the

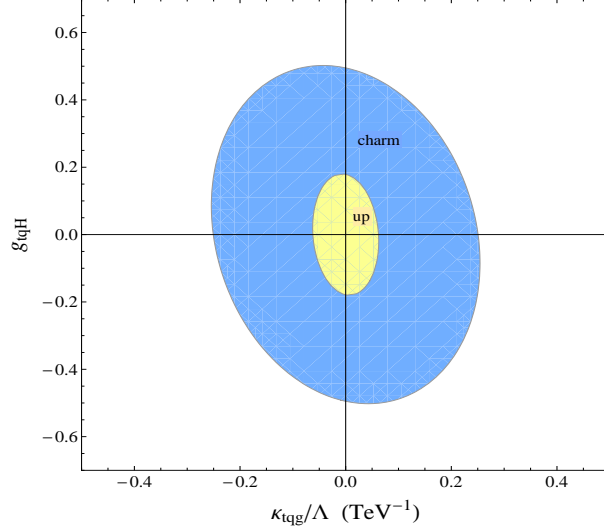


Figure 5: The  $3\sigma$  exclusion upper limits on the anomalous couplings  $\frac{\kappa_{tqg}}{\Lambda}$  and  $g_{tqH}$  for  $10 \text{ fb}^{-1}$  of integrated luminosity at the LHC with the center-of-mass energy of 14 TeV.

top/antitop asymmetry is directly translated in a corresponding lepton charge asymmetry. This is a reasonable assumption because the efficiencies of lepton selection and also fake charged lepton contamination are almost independent of charge. The dominant background to our signal is  $t\bar{t}$  which is charge symmetric at leading order. However, when the next-to-leading order corrections are included anti-top quarks prefer to be more central than the top quarks. Therefore, more leptons will be observed than anti-leptons in the central region of the detector. The magnitude of this charge asymmetry is estimated to be around 1% [42]. QCD multi-jet background is expected to be perfectly charge-symmetric [43]. The only background which has charge asymmetry among the main backgrounds is  $W + jets$ . This nice feature of signal provides the possibility of reaching the signal in the form of an excess in the ratio of positive to negative leptons after subtraction of the expected contribution of the  $W + jets$  background. In such analysis one has to take into account the possibility of charge mis-measurement as well as any potential differences in efficiency between the positive and negative leptons. However, these are expected to be negligible in particular for muons. In this analysis, we define a ratio  $R$  as the number of events with positive charged lepton to the number of events with negative charge. The inclusive values of  $R$  for signal,  $W + jets$  ( $W + jjj$  and  $Wb\bar{b}j$ ), and  $t\bar{t}$  are:

$$R_{\text{signal}} = 4.35 \pm 0.02, \quad R_{W+jets} = 1.57 \pm 0.03, \quad R_{t\bar{t}} = 1.04 \pm 0.03 \quad (15)$$

where the uncertainties are only statistical uncertainties. As it can be seen the inclusive value of the charge ratio for signal is significantly larger than the main backgrounds even

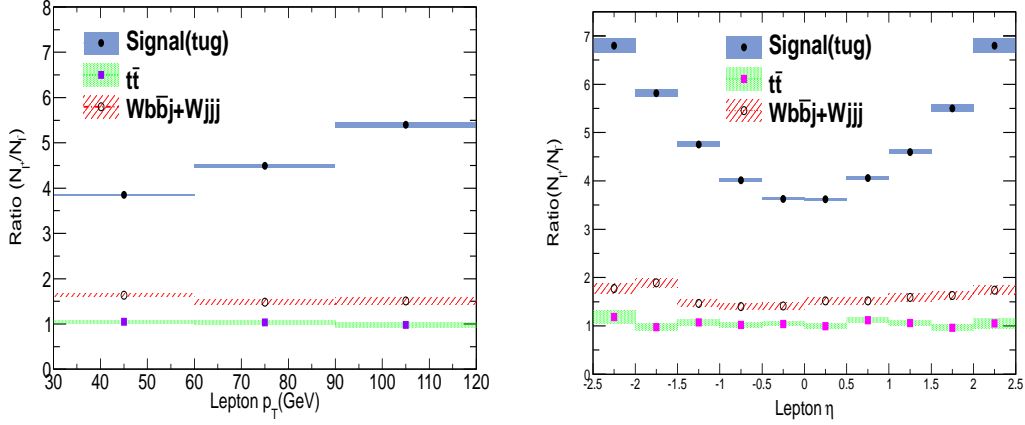


Figure 6: The ratio of positive to negative leptons as a function of lepton  $p_T$  (left) and lepton  $\eta$  (right). The uncertainty is only the statistical one.

around three times larger than the ratio of the charge asymmetric  $W + jets$  background. It is important to note that the value of  $R$  for signal is independent of the value of the anomalous couplings  $\kappa_{tug}/\Lambda$ . Similar feature exists for direct top production due to anomalous  $tqq$  couplings which has been discussed in [15]. In addition to the inclusive value of the charge ratio, we investigate the dependence of the charge ratio  $R$  for the signal and main backgrounds on the transverse momentum and pseudorapidity of the charged lepton. Figure 6 shows the charge ratio  $R$  as a function of lepton  $p_T$  (left) and lepton  $\eta$  (right). As it can be seen,  $R$  grows with increasing the lepton  $p_T$  for signal while it is almost flat for  $t\bar{t}$  and  $W + jets$  backgrounds. The charge ratio is around 3.8 for low  $p_T$  leptons while it goes up to 5.4 for very energetic charged leptons. This behavior can be understood by considering the fact that the high  $p_T$  lepton in the final state needs larger fraction of the parton momentum from the proton PDF. It is well-known that the up quark PDF are much larger than the anti-up quark PDF at large values of  $x$  ( $x$  is the fraction of the proton momentum which a parton carries). Thus, at large lepton  $p_T$ , larger ratio is expected.

The ratio  $R$  as a function of lepton  $\eta$  is depicted in the right side of Figure 6. Again for top pair events the ratio is almost flat and fluctuating around one while for  $W + jets$  is very slowly increasing with  $|\eta|$ . For the signal,  $R$  starts from 3.5 at  $\eta \sim 0$  and grows significantly up to 6.8 at  $2.0 \leq |\eta| \leq 2.5$ . It is apparent that the ratio  $R(p_T)$  and  $R(\eta)$  has a strong discriminating power between signal and the main backgrounds. The increasing behavior of the charge ratio with  $|\eta|$  can be understood by looking at Fig.7. As it can be seen in this figure, there is an apparent correlation between  $p_T$  and  $\eta$  of the charged lepton for the signal events. Higher lepton  $p_T$  events are correlated with larger lepton  $\eta$ . Therefore,

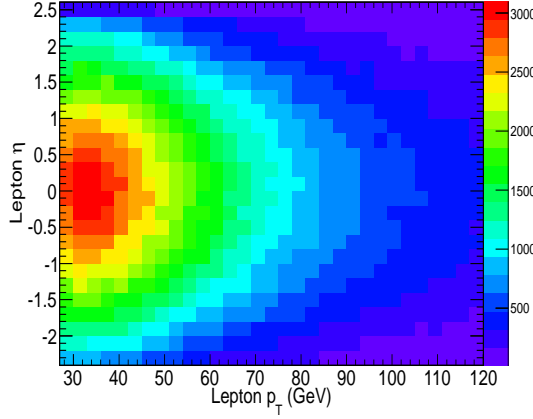


Figure 7: The correlation between the transverse momentum and pseudorapidity of the charged lepton for signal events.

the large charge ratio for very energetic lepton would lead to the large charge ratio in the forward/backward region. Indeed, there is a correlation between  $R(p_T)$  and  $R(\eta)$ .

It is important to note that the charge ratio is sensitive to the choice of parton distribution function (PDF) of the proton. In [43], the CMS Collaboration has measured the charge ratio in single top  $t$ -channel. The largest source of systematic uncertainty on the ratio is coming from the limited knowledge of proton PDF. In this work, we have estimated the the uncertainties due to PDF by using the 44 members of the CTEQ6.6 PDFs. We have found that the relative uncertainty due to PDF on the ratio  $R$  is around  $\Delta R/R = 7\%$ . The PDF uncertainty on the ratio  $R$  varies in bins of the lepton  $\eta$ . For the central leptons the PDF uncertainty is around 3% which increases up to around 6 – 7% for the leptons in the forward/backward region. We also varied the factorization and renormalization scale to find uncertainty on the charge ratio. It is found to be less than 1%.

Apart from the ability of the charge ratio to discriminate between signal and backgrounds, upon the signal discovery it can be used to determine that the signal comes from  $t - u - g$  coupling or  $t - c - g$  couplings. Since the  $t - c - g$  anomalous coupling has equal contribution in top and anti-top production the inclusive and the differential charge ratio ( $R(p_T)$  and  $R(\eta)$ ) have quite different values and behaviors with the case that the signal originates from  $t - u - g$  anomalous coupling.

It is notable that similar charge ratio properties as mentioned in this section is applicable on the other channels of anomalous single top production in association with a vector boson or a Higgs boson. Processes like  $q + g \rightarrow t + \gamma$  (with anomalous interaction of  $tq\gamma$  and  $tqg$ ) and  $q + g \rightarrow t + H$  (with anomalous couplings of  $tqH$  and  $tqg$ ) and also  $q + g \rightarrow t + Z$  (with

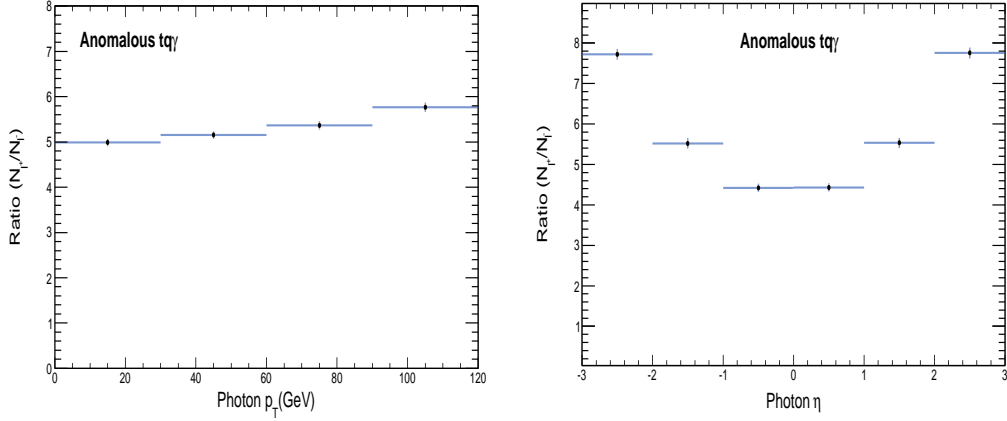


Figure 8: The ratio of anti-lepton to lepton as a function of photon  $p_T$  (left) and photon  $\eta$  (right).

anomalous interaction of  $tqZ$  and  $tqg$ ) [16], [17], [18]. As an example, we show the charge ratio in the process of  $q + g \rightarrow t + \gamma$  (with  $tq\gamma$  anomalous interaction) as a function of photon  $p_T$  and  $\eta$  in Fig.8. An increasing behavior for the charge ratio at large photon transverse momentum and large rapidities can be seen.

## 6 Conclusions

In this work we propose to use the  $pp \rightarrow t(\bar{t}) + H$  process to probe the anomalous  $tug$  and  $tcg$  couplings as a complementary channel besides the other channels. We concentrate on the leptonic decay of the top quark and the Higgs boson decay to  $b\bar{b}$  at the LHC with the center-of-mass energy of 14 TeV. A set of kinematic variables have been proposed to discriminate between the signal from backgrounds. After applying the selection, we show that the LHC can probe the anomalous  $tug(tcg)$  couplings down to 0.01 (0.04)  $\text{TeV}^{-1}$  with  $10 \text{ fb}^{-1}$  of integrated luminosity. We also study the production of a single top quark plus a Higgs boson coming from  $tqg$  and  $tqH$  anomalous couplings at the same time and derive the  $3\sigma$  exclusion upper limits on the strengths of the anomalous couplings. We propose the charge ratio versus transverse momentum and the pseudorapidity of the charge lepton as a strong tool to discriminate between signal and backgrounds as well as its ability to distinguish between the anomalous couplings  $tug$  and  $tcg$ . We have shown that in particular in the high- $p_T$  region or for the leptons in the forward/backward regions, the charge ratio increases significantly. We have found that the charge ratio is robust against the variation of PDF and  $Q$ -scale.

## References

- [1] F. -P. Schilling, Int. J. Mod. Phys. A **27**, 1230016 (2012) [arXiv:1206.4484 [hep-ex]].
- [2] W. Bernreuther, arXiv:0805.1333 [hep-ph].
- [3] The ATLAS Collaboration, ATLAS-CONF-2012-132.
- [4] The ATLAS Collaboration, ATLAS-CONF-2012-024.
- [5] S. L. Glashow, J. Iliopoulos and L. Maiani, Phys. Rev. D **2**, 1285 (1970).
- [6] T. M. P. Tait and C. -P. Yuan, Phys. Rev. D **63**, 014018 (2000) [hep-ph/0007298].
- [7] J. A. Aguilar-Saavedra, Acta Phys. Polon. B **35**, 2695 (2004) [hep-ph/0409342].
- [8] J. J. Liu, C. S. Li, L. L. Yang and L. G. Jin, Phys. Lett. B **599**, 92 (2004) [hep-ph/0406155].
- [9] S. Bejar, J. Guasch, D. Lopez-Val and J. Sola, Phys. Lett. B **668**, 364 (2008) [arXiv:0805.0973 [hep-ph]].
- [10] J. Cao, Z. Heng, L. Wu and J. M. Yang, Phys. Rev. D **79**, 054003 (2009) [arXiv:0812.1698 [hep-ph]]; R. Guedes, R. Santos and M. Won, arXiv:1308.4723 [hep-ph].
- [11] G. A. Gonzalez-Sprinberg and R. Martinez, hep-ph/0605335; R. Coimbra, A. Onofre, R. Santos and M. Won, Eur. Phys. J. C **72**, 2222 (2012) [arXiv:1207.7026 [hep-ph]].
- [12] J. A. Aguilar-Saavedra and B. M. Nobre, Phys. Lett. B **553**, 251 (2003) [hep-ph/0210360]; G. Eilam, J. L. Hewett and A. Soni, Phys. Rev. D **44**, 1473 (1991) [Erratum-ibid. D **59**, 039901 (1999)].
- [13] E. Malkawi and T. M. P. Tait, Phys. Rev. D **54**, 5758 (1996) [hep-ph/9511337].
- [14] M. Hosch, K. Whisnant and B. L. Young, Phys. Rev. D **56**, 5725 (1997) [hep-ph/9703450]; J. A. Aguilar-Saavedra, Nucl. Phys. B **812**, 181 (2009) [arXiv:0811.3842 [hep-ph]].
- [15] J. Gao, C. S. Li, L. L. Yang and H. Zhang, Phys. Rev. Lett. **107**, 092002 (2011) [arXiv:1104.4945 [hep-ph]].



- [16] Y. Wang, F. P. Huang, C. S. Li, B. H. Li, D. Y. Shao and J. Wang, Phys. Rev. D **86**, 094014 (2012) [arXiv:1208.2902 [hep-ph]].
- [17] The CMS Collaboration, CMS-PAS-TOP-12-021.
- [18] J. -L. Agram, J. Andrea, E. Conte, B. Fuks, D. Gel and P. Lansonneur, Phys. Lett. B **725**, 123 (2013) [arXiv:1304.5551 [hep-ph]]; J. A. Aguilar-Saavedra, Nucl. Phys. B **837**, 122 (2010) [arXiv:1003.3173 [hep-ph]].
- [19] N. Kidonakis and A. Belyaev, JHEP **0312**, 004 (2003) [hep-ph/0310299]; P. M. Ferreira, O. Oliveira and R. Santos, Phys. Rev. D **73**, 034011 (2006) [hep-ph/0510087]; J. A. Aguilar-Saavedra and G. C. Branco, Phys. Lett. B **495**, 347 (2000) [hep-ph/0004190].
- [20] S. M. Etesami and M. Mohammadi Najafabadi, Phys. Rev. D **81**, 117502 (2010) [arXiv:1006.1717 [hep-ph]]; M. Khatiri Yanehsari, S. Jafari and M. Mohammadi Najafabadi, Int. J. Theor. Phys. **52**, 4229 (2013).
- [21] J. J. Zhang, C. S. Li, J. Gao, H. Zhang, Z. Li, C. -P. Yuan and T. -C. Yuan, Phys. Rev. Lett. **102**, 072001 (2009) [arXiv:0810.3889 [hep-ph]].
- [22] T. Aaltonen *et al.* [CDF Collaboration], Phys. Rev. Lett. **102**, 151801 (2009) [arXiv:0812.3400 [hep-ex]].
- [23] V. M. Abazov *et al.* [D0 Collaboration], Phys. Lett. B **693**, 81 (2010) [arXiv:1006.3575 [hep-ex]].
- [24] The ATLAS collaboration, ATLAS-CONF-2013-063
- [25] G. Aad *et al.* [ATLAS Collaboration], Phys. Lett. B **716**, 1 (2012) [arXiv:1207.7214 [hep-ex]].
- [26] S. Chatrchyan *et al.* [CMS Collaboration], Phys. Lett. B **716**, 30 (2012) [arXiv:1207.7235 [hep-ex]].
- [27] A. Fernandez, C. Pagliarone, F. Ramirez-Zavaleta and J. J. Toscano, J. Phys. G **37**, 085007 (2010) [arXiv:0911.4995 [hep-ph]].
- [28] F. Larios, R. Martinez and M. A. Perez, Phys. Rev. D **72**, 057504 (2005) [hep-ph/0412222].

- [29] J. Alwall, M. Herquet, F. Maltoni, O. Mattelaer and T. Stelzer, JHEP **1106**, 128 (2011) [arXiv:1106.0522 [hep-ph]].
- [30] J. Pumplin, D. R. Stump, J. Huston, H. L. Lai, P. M. Nadolsky and W. K. Tung, JHEP **0207**, 012 (2002) [hep-ph/0201195].
- [31] T. Sjostrand, S. Mrenna and P. Z. Skands, Comput. Phys. Commun. **178**, 852 (2008) [arXiv:0710.3820 [hep-ph]].
- [32] M. Cacciari and G. P. Salam, Phys. Lett. B **641**, 57 (2006) [hep-ph/0512210].
- [33] M. Cacciari, G. P. Salam and G. Soyez, JHEP **0804**, 063 (2008) [arXiv:0802.1189 [hep-ph]].
- [34] N. D. Christensen and C. Duhr, Comput. Phys. Commun. **180**, 1614 (2009) [arXiv:0806.4194 [hep-ph]].
- [35] C. Duhr and B. Fuks, Comput. Phys. Commun. **182**, 2404 (2011) [arXiv:1102.4191 [hep-ph]].
- [36] C. Degrande, C. Duhr, B. Fuks, D. Grellscheid, O. Mattelaer and T. Reiter, Comput. Phys. Commun. **183**, 1201 (2012) [arXiv:1108.2040 [hep-ph]].
- [37] E. Boos *et al.* [CompHEP Collaboration], Nucl. Instrum. Meth. A **534**, 250 (2004) [hep-ph/0403113].
- [38] A. Pukhov, E. Boos, M. Dubinin, V. Edneral, V. Ilyin, D. Kovalenko, A. Kryukov and V. Savrin *et al.*, hep-ph/9908288.
- [39] G. Aad *et al.* [ATLAS Collaboration], arXiv:0901.0512 [hep-ex].
- [40] B. H. Li, Y. Zhang, C. S. Li, J. Gao and H. X. Zhu, Phys. Rev. D **83**, 114049 (2011) [arXiv:1103.5122 [hep-ph]].
- [41] M. Feindt and U. Kerzel, , Nucl. Instrum. Meth. A **559** 190 (2006).
- [42] J. H. Kuhn and G. Rodrigo, JHEP **1201**, 063 (2012) [arXiv:1109.6830 [hep-ph]].
- [43] The CMS Collaboration, CMS-PAS-TOP-12-038.